

國立宜蘭大學
100 學年度轉學招生考試

(考生填寫)
准考證號碼：

工程數學試題

《作答注意事項》

1. 請先檢查准考證號碼、座位號碼及答案卷號碼是否相符。
2. 考試時間：80 分鐘。
3. 本試卷共有 5 題，一題 20 分，共計 100 分。
4. 請將答案寫在答案卷上。
5. 考試中禁止使用大哥大或其他通信設備。
6. 考試後，請將試題卷及答案卷一併繳交。

Using the method described only for each question.

1. (20%) What type of point about x at 0 and 2 for the following equation in the expansion of the power series? (Ordinary, regular singular, or irregular singular)

$$x \frac{d^2 y}{dx^2} + (2-x) \frac{dy}{dx} - y = 0$$

2. (20%) Find a general solution, $\frac{dy}{dx} + \sin(\pi x) = 0$

3. (20%) Find a general solution, using the undetermined coefficients.

$$\frac{d^2 y}{dx^2} + 6 \frac{dy}{dx} + 73y = 80e^x \cos(4x)$$

4. (20%) Find a general solution, using Laplace transform

$$\frac{d^2 y}{dx^2} + 2 \frac{dy}{dx} + 2y = 0, \quad y(0) = 1, \quad \frac{dy(0)}{dx} = -3$$

5. (20%) Find the odd periodic extension of the following function, of period $2L$

$$\begin{aligned} f(x) &= (2/L)x, & 0 < x < L/2 \\ &= (2/L)(L-x), & L/2 < x < L \end{aligned}$$