

Solve the following problems (20% for each problem):

1. $\frac{\partial u}{\partial x} + 2x \frac{\partial u}{\partial t} = 2x$ with $u(x, 0) = 1 ; u(0, t) = t$

2. $y_1'' = y_1 + 1$
 $y_2'' = 2y_1 + 1$

3. $(D^2 - 2D + 1)y = x^2 + x^{-1}$

4. $4xy'' + 2y' + y = 0$

5. $y(3x^2 - ay)dx - x(3x^2 - 2ay)dy = 0$